

Graph Rubbling

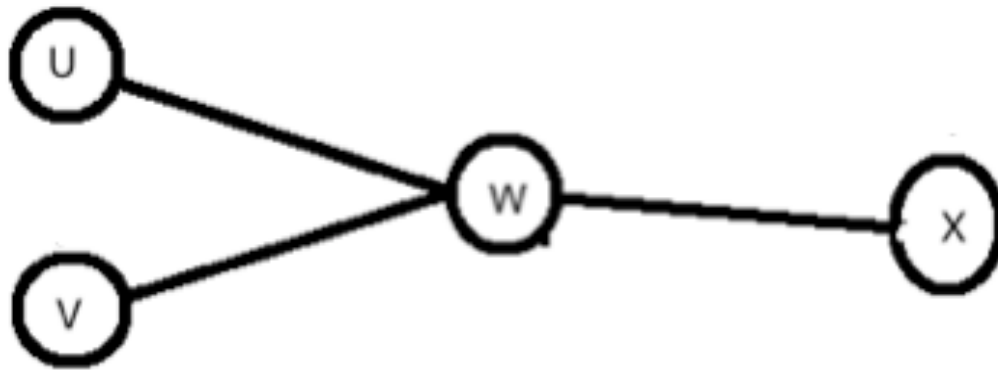
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DIMACS REU

June 7, 2011

Simple, Finite, Undirected Graph G



$$G=(V,E)$$

$$V(G)=\{u,v,w,x\}$$

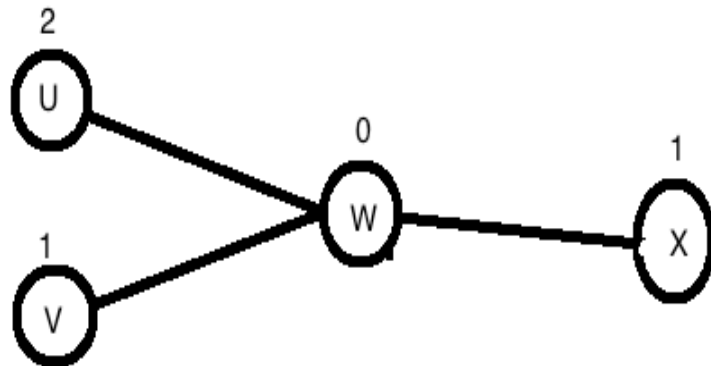
$$E(G)=\{uw,vw,xw\}$$

Pebble Distribution

A pebble distribution, p , is a nonnegative pebble function.

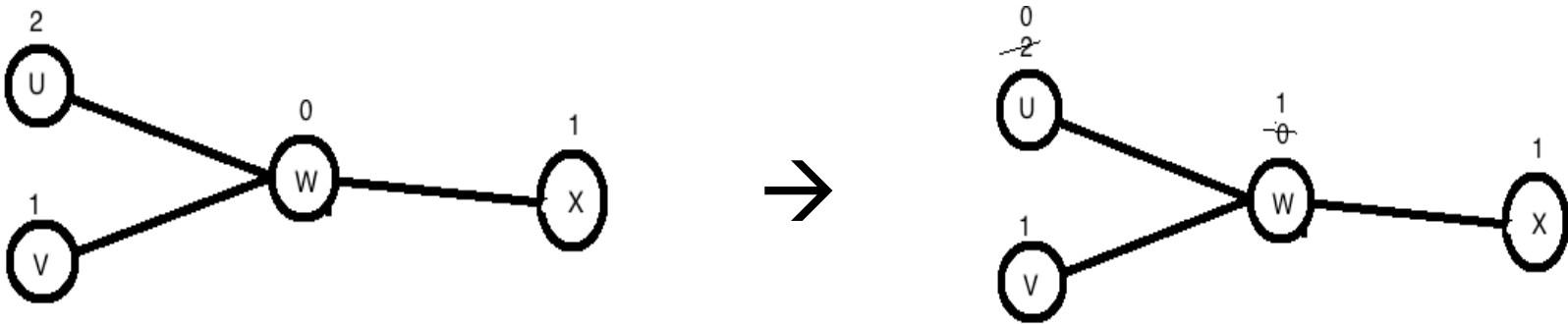
The size of the p is all the pebbles on the graph.

Pebble Function	
$V(G)$	$p(V(G))$
u	2
v	1
w	0
x	1



Pebbling Move

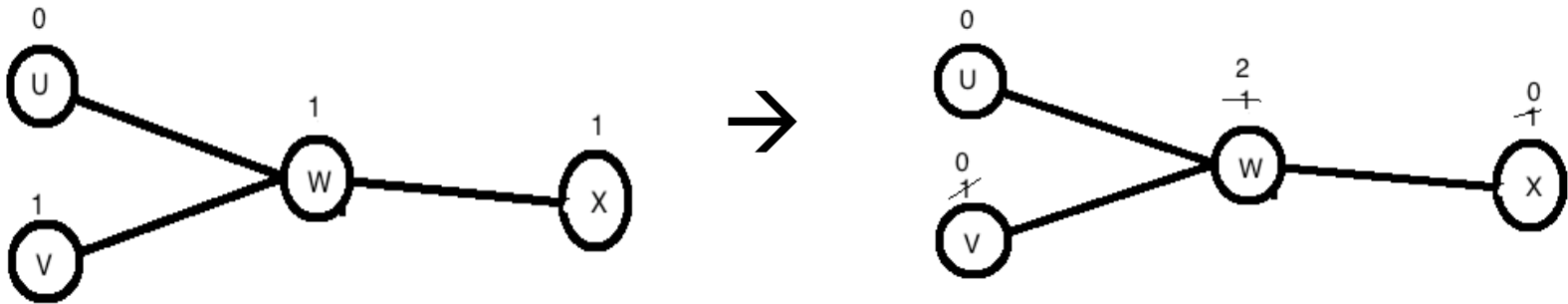
A pebbling move in a graph removes two pebbles at a vertex and adds one pebble at an adjacent vertex.



After pebbling move($u \rightarrow w$), it forms a new distribution.

Rubbling Moves

A strict rubbling move removes one pebble from each of x and v , and adds one pebble on w .



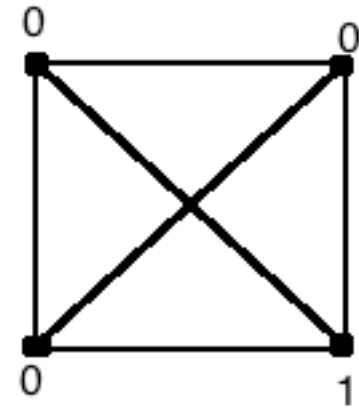
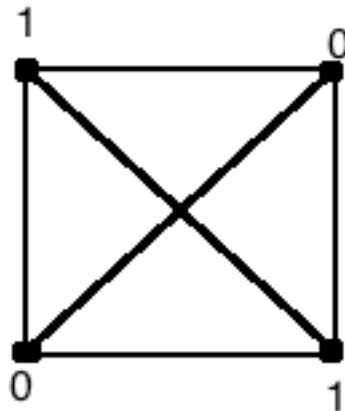
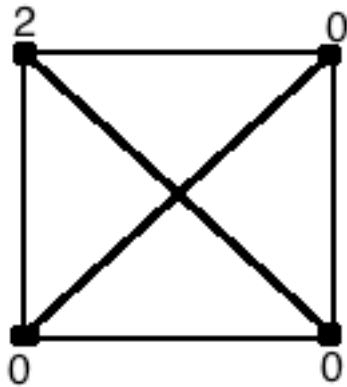
Rubbling move $r=(v,x \rightarrow w)$

Rubbling moves include both pebbling moves and strict rubbling moves.

Rubbling Number of Graph

The rubbling number $\rho(G)$, of a graph is the minimum number m that every vertex of G is reachable from any pebble distribution of size m .

For example ; $\rho(K_4)=2$



Few Facts about Rubbling

- $\rho(K_n)=2$, where K_n is the complete graph ($n \geq 2$)
- $\rho(W_n)=4$ where W_n is the wheel graph ($n \geq 5$)
- $\rho(C_{2k})=2^k$, where C_{2k} is an even cycle.
- $2^{\text{diam}(G)} \leq \rho(G)$

My Research Direction

Learning the results from the graph pebbling ,we will reproduce the pebbling results in terms of rubbing ,especially for the family of trees.

Thanks!

